

SYBSc SEMESTER IV
MATHS II
SAMPLE QUESTIONS

1.

Let G be a group and $a, b, c \in G$ then the solution of the equations $axb^{-1} = c$ and $a^{-1}y^{-1}b^{-1} = c$ are

- (a) $x = a^{-1}c^{-1}b, y = a^{-1}c^{-1}b^{-1}$ (b) $x = a^{-1}c, y = a^{-1}c^{-1}b^{-1}$
 (c) $x = b^{-1}c^{-1}a^{-1}, y = a^{-1}c^{-1}b^{-1}$ (d) $x = a^{-1}c, y = b^{-1}c^{-1}a^{-1}$

2.

Consider the set $G = \{\bar{5}, \bar{15}, \bar{25}, \bar{35}\}$ under multiplication of residue classes modulo 40.

Then

- (a) G is not a group as $\bar{1} \notin G$ (b) G is a group with $\bar{25}$ as identity
 (c) G is a group with $\bar{5}$ as identity (d) None of these

3.

For what value of $n, D_n = S_n$

- (a) $n=3$ (b) $n=4$
 (c) $n=5$ (d) No such n exists

4.

Let G be a group having elements of order 1,2,3,4,5,6. The minimal possible order G of is

- (a) 100 (b) 30
 (c) 60 (d) 1

5.

Let G be a non-Abelian group $Z(G) = \{x \in G / ax = xa, \forall a \in G\}$ then

- (a) $Z(G) = \{e\}$ (b) $Z(G) \neq G$ and $Z(G)$ is abelian
 (c) $Z(G) = G$ (d) $Z(G)$ is non-abelian

6.

Number of elements of order 5 in Z_{1000} is

- (a) 1 (b) 4
 (c) 5 (d) 200

7.

Let G be a cyclic group of order n generated by 'a' then $\langle a^r \rangle = \langle a^s \rangle$ implies

- (a) $(r,s)=1$ (b) $S=(n,r)$
 (c) $(n,r)=(n,s)$ (d) $(r|(n,s))$

8.

Let H be a subgroup of G and $a, b \in G$ If then $aH \neq bH$ then

- (a) $aH \cap bH = \emptyset$ (b) $aH \cap bH \neq \emptyset$
 (c) $aH \subset bH$ (d) $aH \supset bH$

9.

Let H be a subgroup of G and $a \in G$. aH is a subgroup of G if and only if

- (a) $a \notin H$ (b) $a \in H$
 (c) $a^{-1} \notin H$ (d) None of these

10. If $G = \mathbb{Z}$ with addition and $H = \{0, \pm 3, \pm 6, \pm 9, \dots\}$ then which of the following is true

(a) $11+H = 17+H$

(b) $11+H = 13+H$

(c) $7+H = 23+h$

(d) $H = H+2$